

# Van Allen Probes and Mass Density Monitoring

Kyungguk Min<sup>1</sup>, Jacob Bortnik<sup>1,3</sup>, Andrew J. Gerrard<sup>1</sup>,  
Jeongwoo Lee<sup>1</sup>, Craig Kletzing<sup>2</sup>

1. CSTR, NJIT, USA

2. UIOWA, USA

3. UCLA, USA

\* We acknowledge the entire EMFISIS team for providing data.

Van Allen Probes SWG meeting  
Feb 2013

# Plasma Mass Density, $\rho$

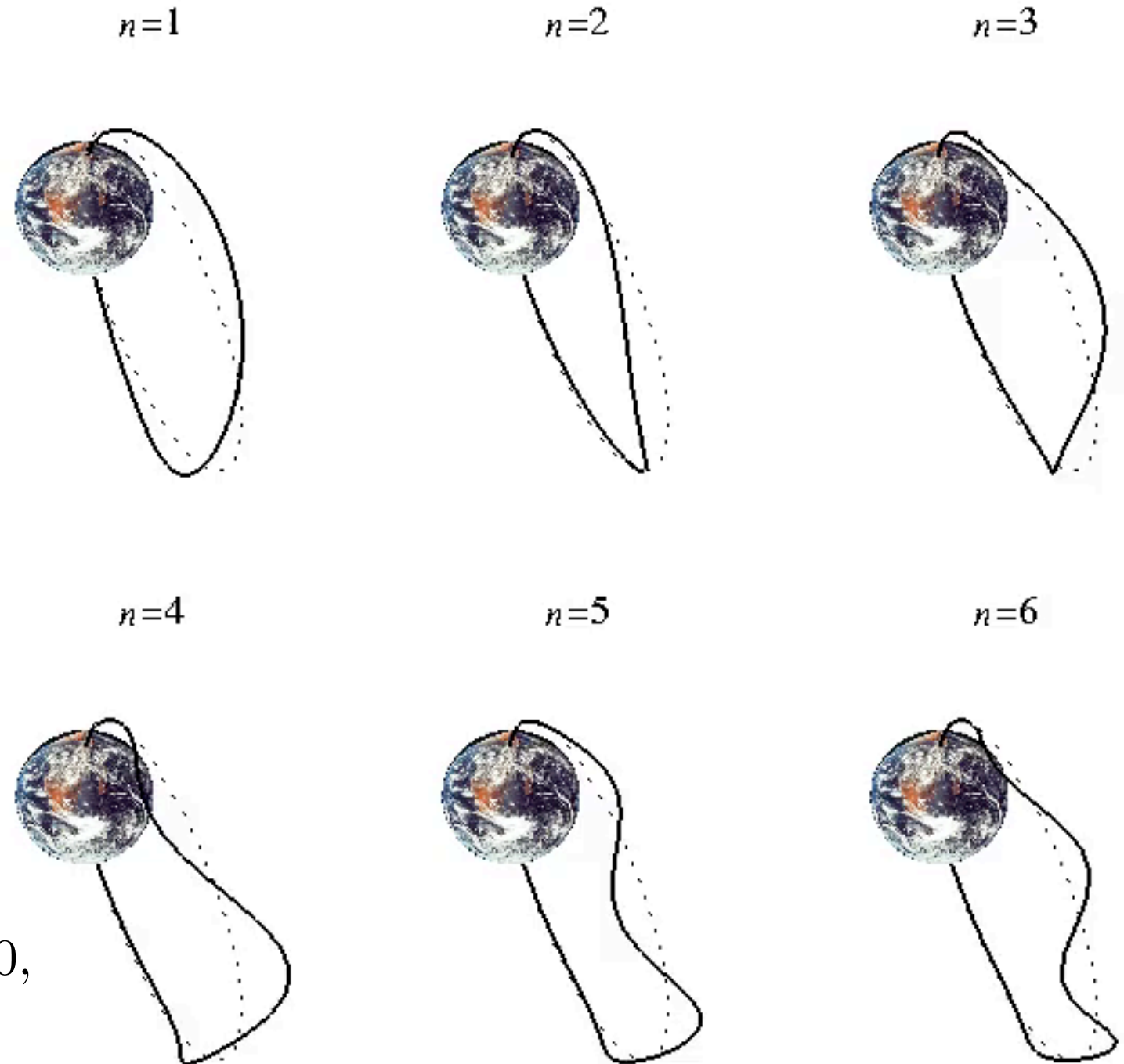
- The most fundamental quantity
  - Serves as a medium that sustains plasma waves
  - Controls the time response of the magnetosphere to internal and external force
  - Controls coulomb collision
- Direct measurement is difficult as opposed to electron density.
- Alternative: Infer  $\rho$  from the toroidal mode Alfvén waves
  - Technique has been refined for several decades
  - Added advantage: full field line mass variation can be resolved
- Van Allen Probes can monitor the plasma mass density

# Magneto-seismology

- Standing waves
  - Tension =  $B$
  - Mass = plasma ( $\rho$ )
- $B$  and  $\rho$  ( $V_A \sim B/\sqrt{\rho}$ )  $\rightarrow$  complete set of resonant  $f$
- Conversely, resonant  $f$  and  $B \rightarrow \rho$
- Analogous to seismology

$$\frac{\partial^2}{\partial s^2} \xi' + \frac{\partial}{\partial s} (\ln(h^2 B)) \frac{\partial}{\partial s} \xi' + \frac{\omega^2}{V_A^2} \xi' = 0,$$

Singer et al. [1981]



# EMFISIS and Toroidal Waves

– EMFISIS L3 1sec Bsm Oct 13 ~ Nov 17 (about 95 orbits per SC)

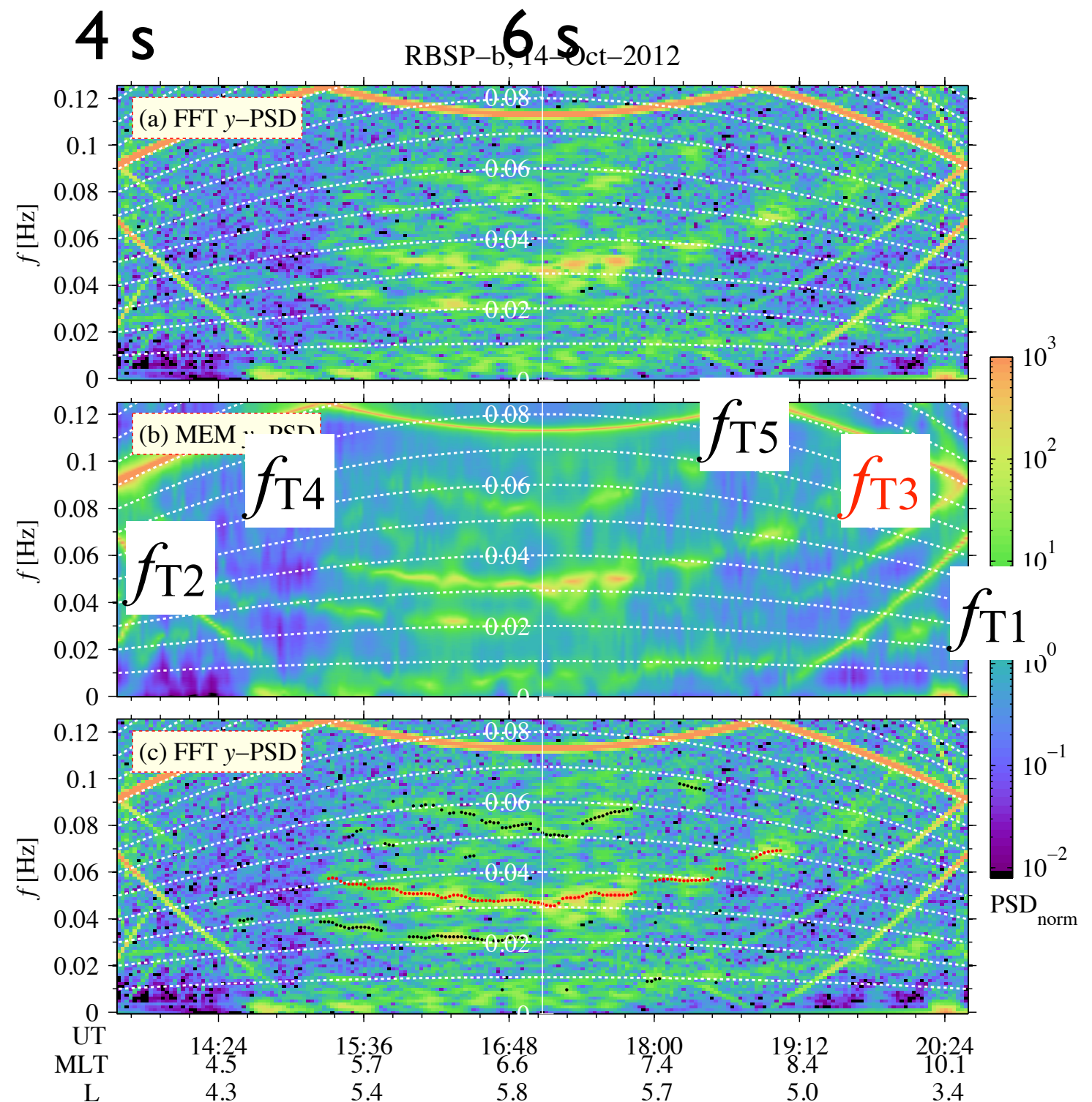
– Data processing following Takahashi et al. [2007, 2010]

– Adaptive sampling

– Maximum Entropy Method gives well defined peaks

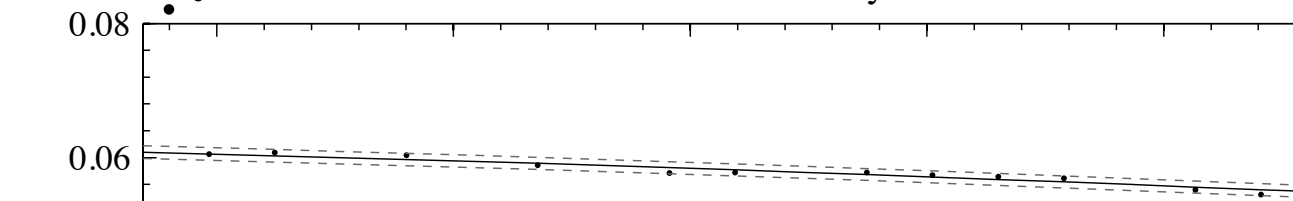
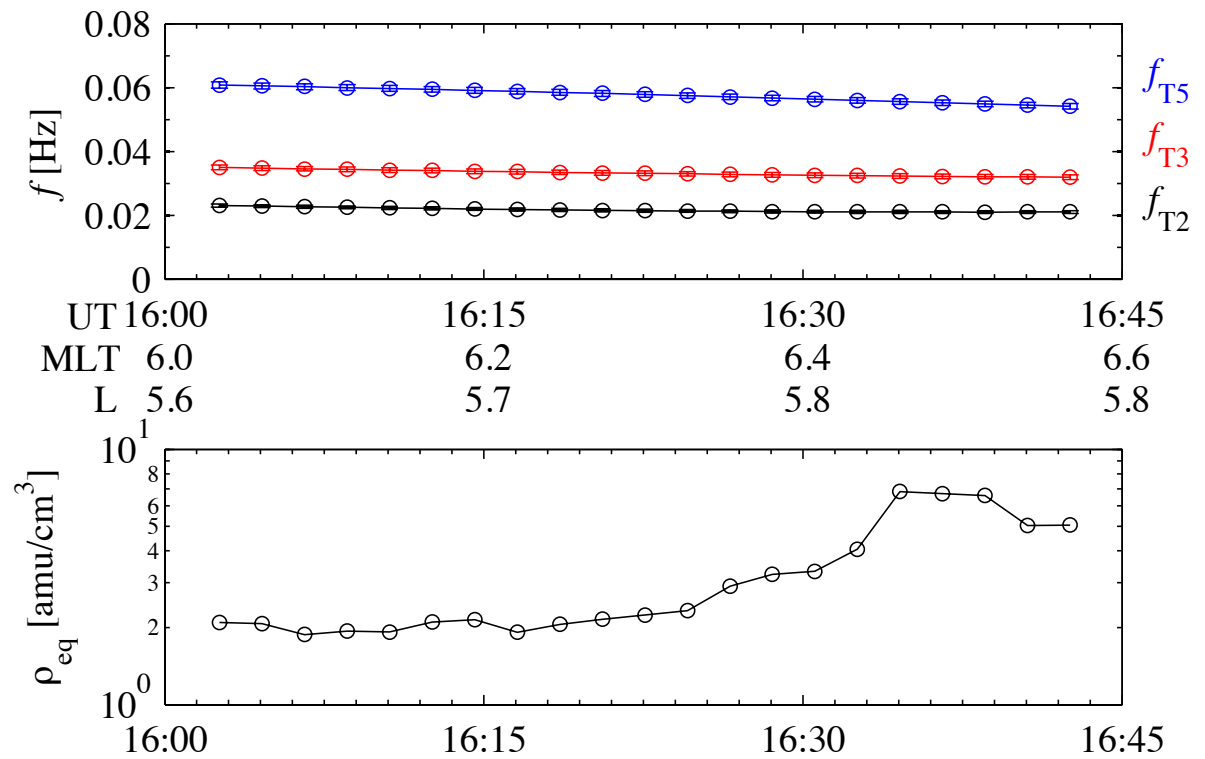
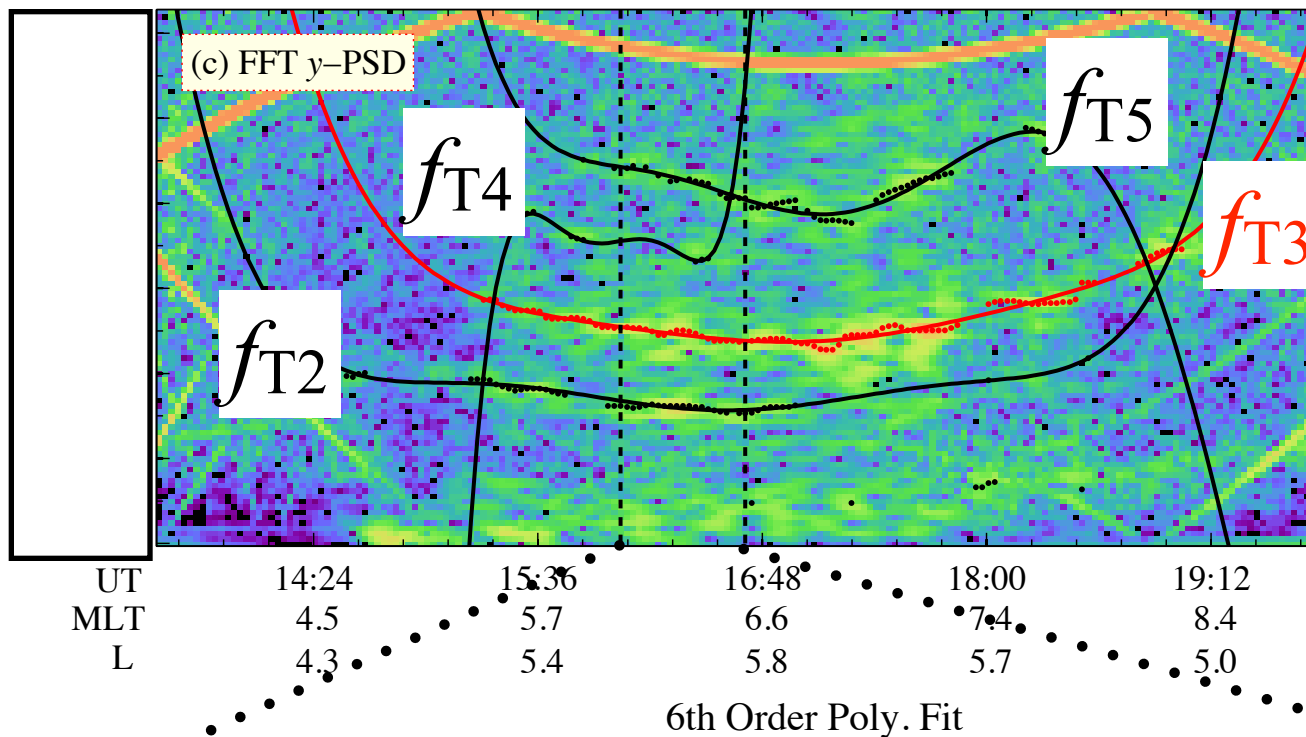
– Criteria [Takahashi et al., 2007, 2010]:

1.  $P_{yy}(f_T) > P_{zz}(f_T)$
2.  $P_{yy}(f_T) > 3 P_{xx}(f_T)$
3.  $\Delta f_T$  (FWHM) < 3 mHz



# Mass Density Inversion for Event 2012-10-14 RBSP-B

RBSP-b, 14-Oct-2012



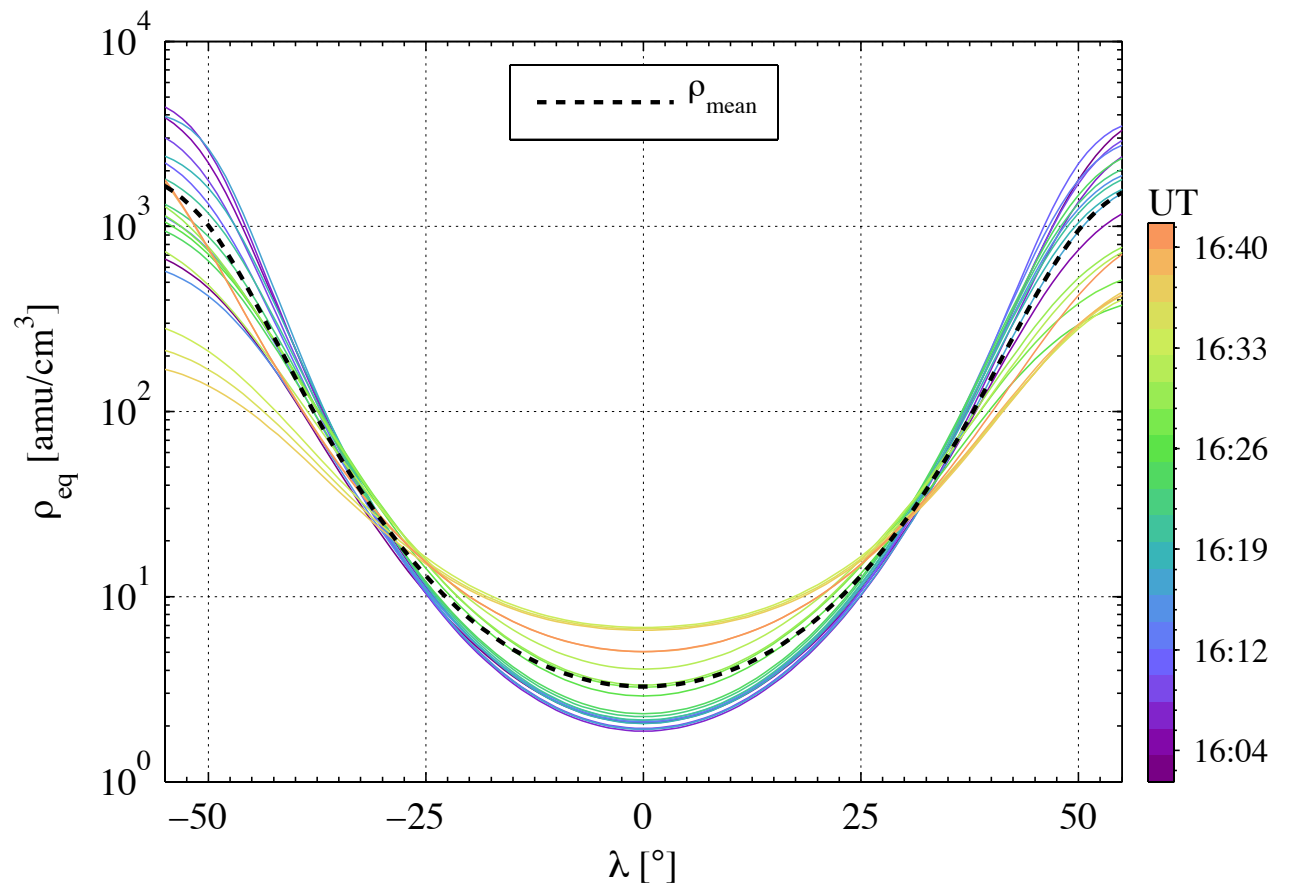
•  $\rho(\lambda)$  Model:

$$\log_{10} \rho = c_0 + c_2 \tau^2 + c_4 \tau^4 + \dots$$

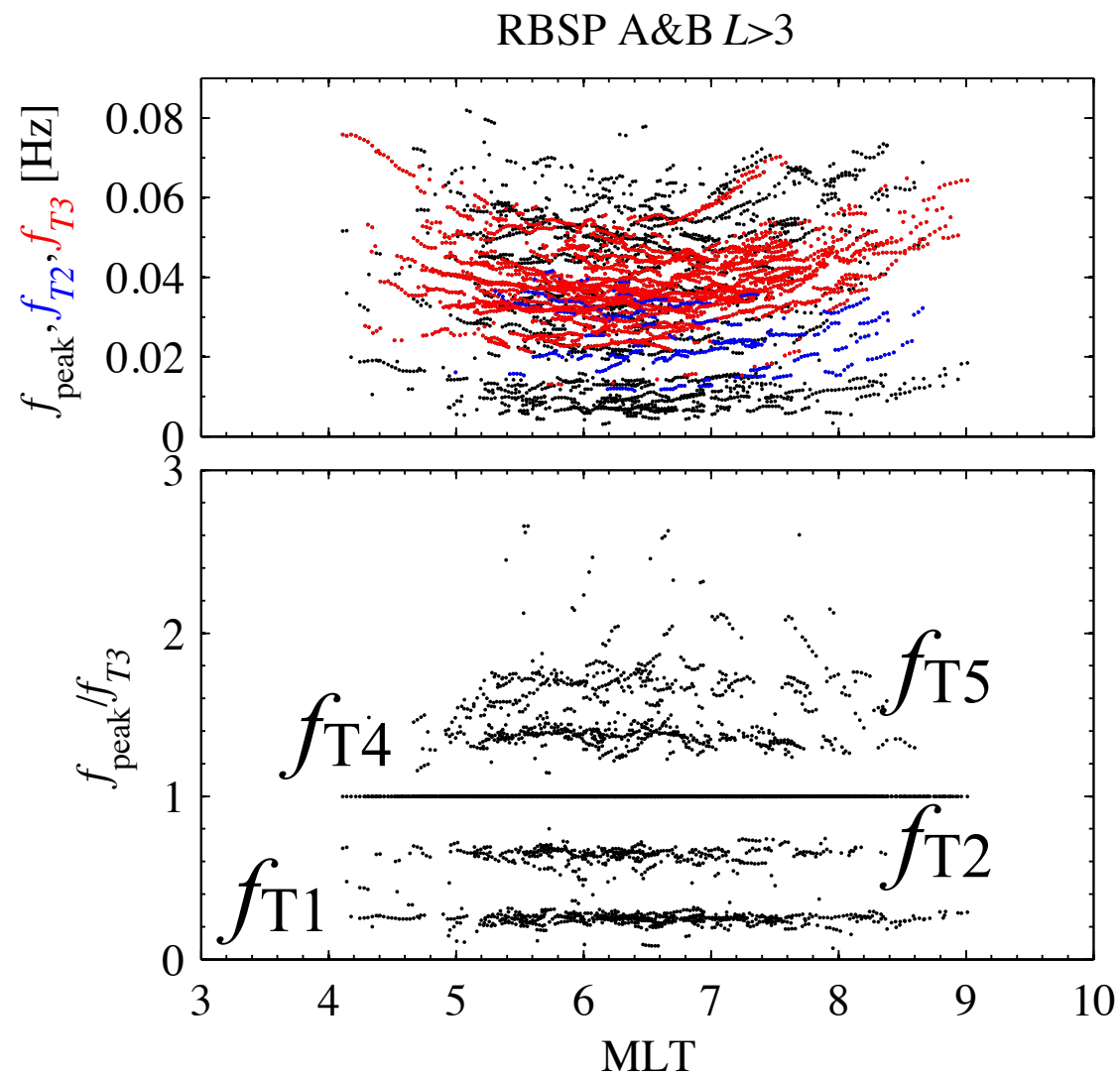
$$\tau \equiv \int \frac{ds}{V_A}$$

Alfvén crossing time

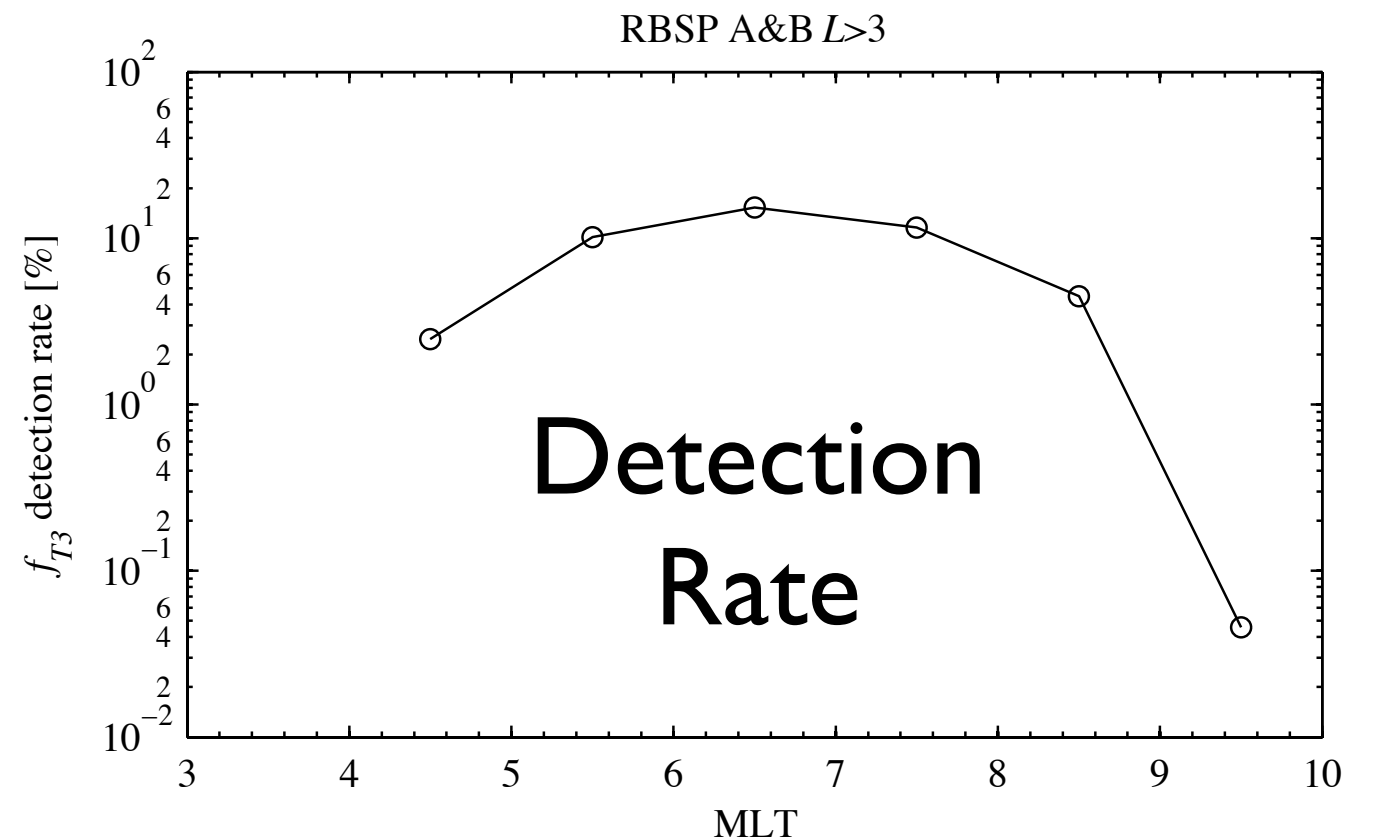
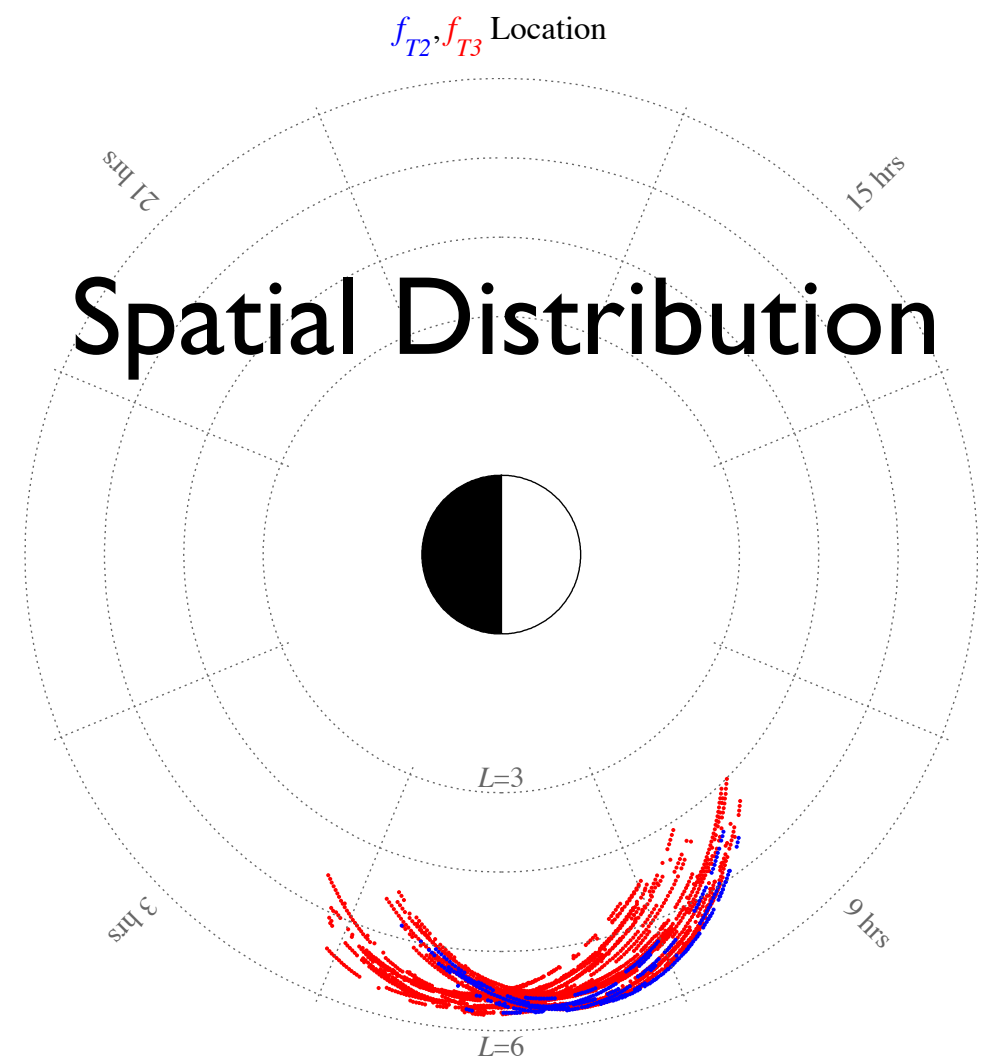
Denton et al. [2001, 2004]



# Toroidal Frequencies: (~ 95 orbits per SC)



## Harmonic Structure



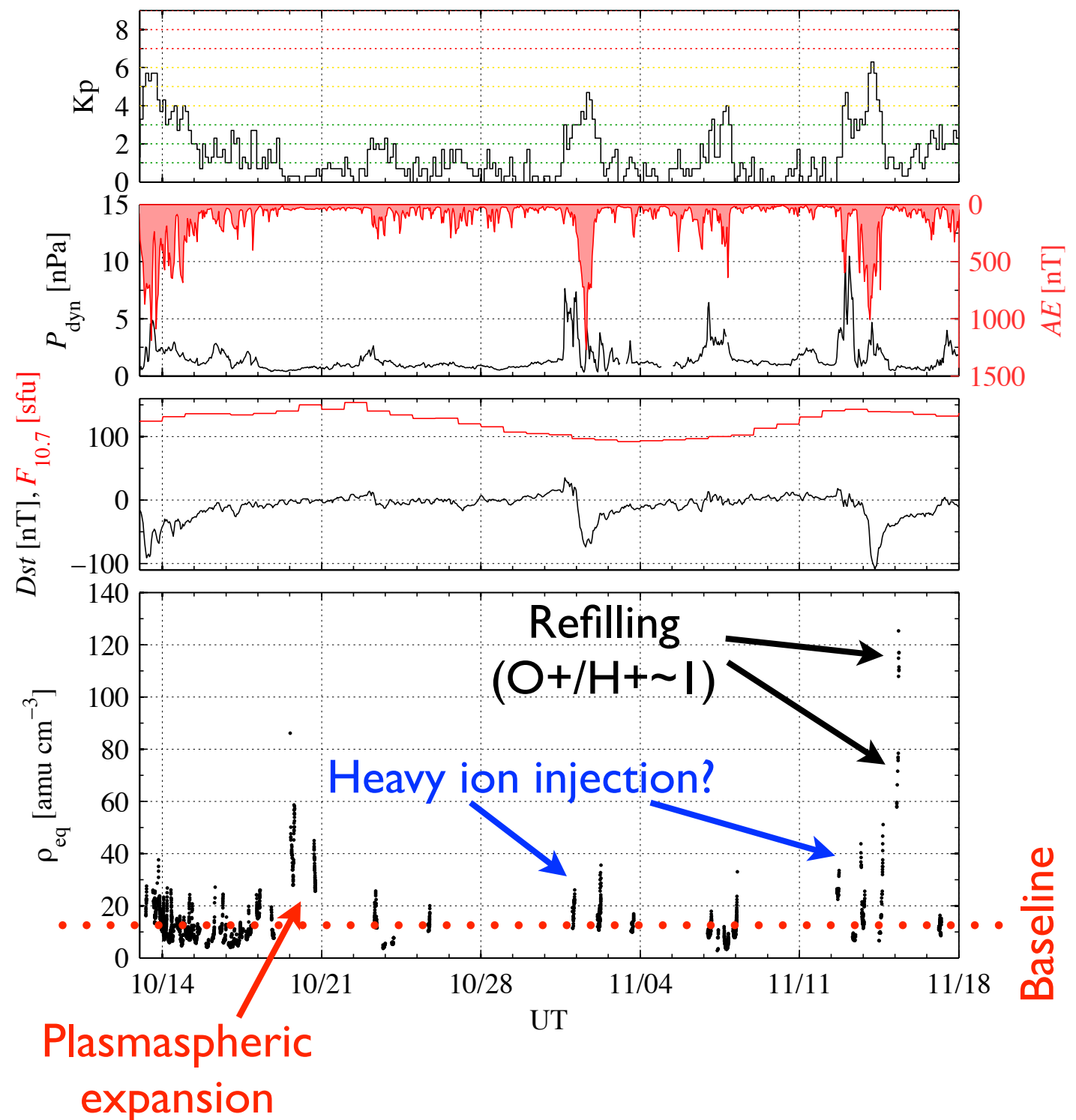
# Equatorial Mass Density, $\rho_{\text{eq}}$

$$\rho = \rho_{\text{eq}} \left( \frac{LR_{\text{E}}}{R} \right)^{\alpha}$$

with  $\alpha = 1$  (e.g. Denton et al. 2006)

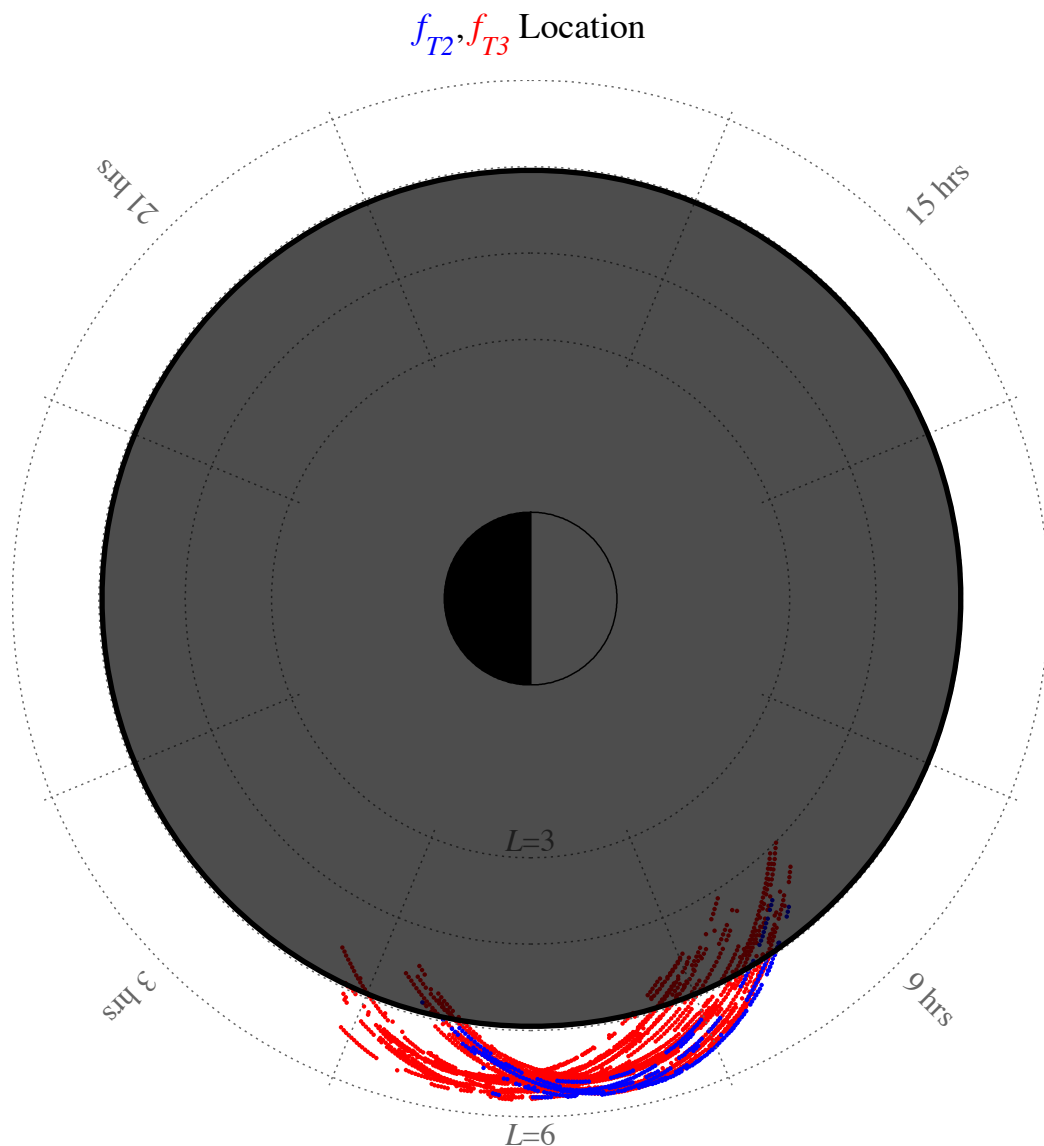
## $\rho_{\text{eq}}$ from RBSP

RBSP A&B  $\rho_{\text{eq}}(t, L>3)$ : 13-Oct-2012 ~ 18-Nov-2012





# Statistical $\rho(\lambda)/\rho_{\text{eq}}$ Variation



- Use samples from all MLT but  $5 < L < 6$
- $\rho(\lambda)$  Model:

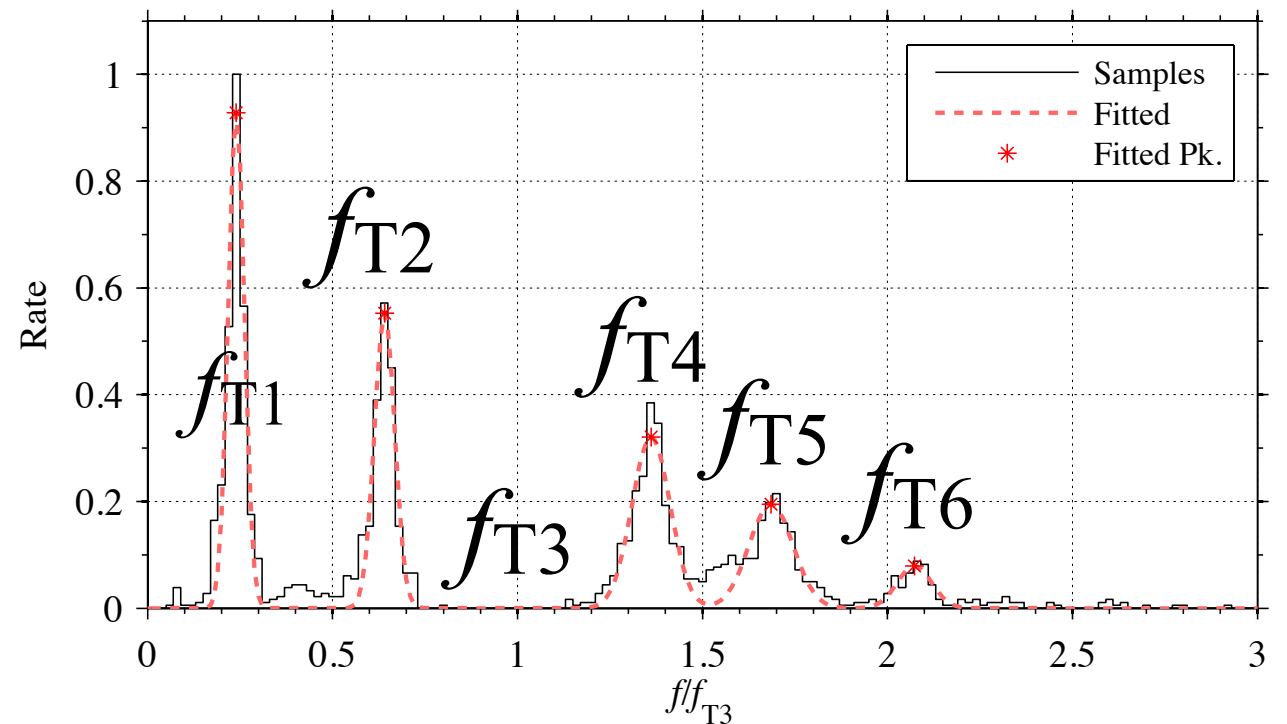
$$\log_{10} \rho = c_2 \tau^2 + c_4 \tau^4 + \dots$$

$$\tau \equiv \int \frac{ds}{V_A} \quad \text{Alfvén crossing time}$$

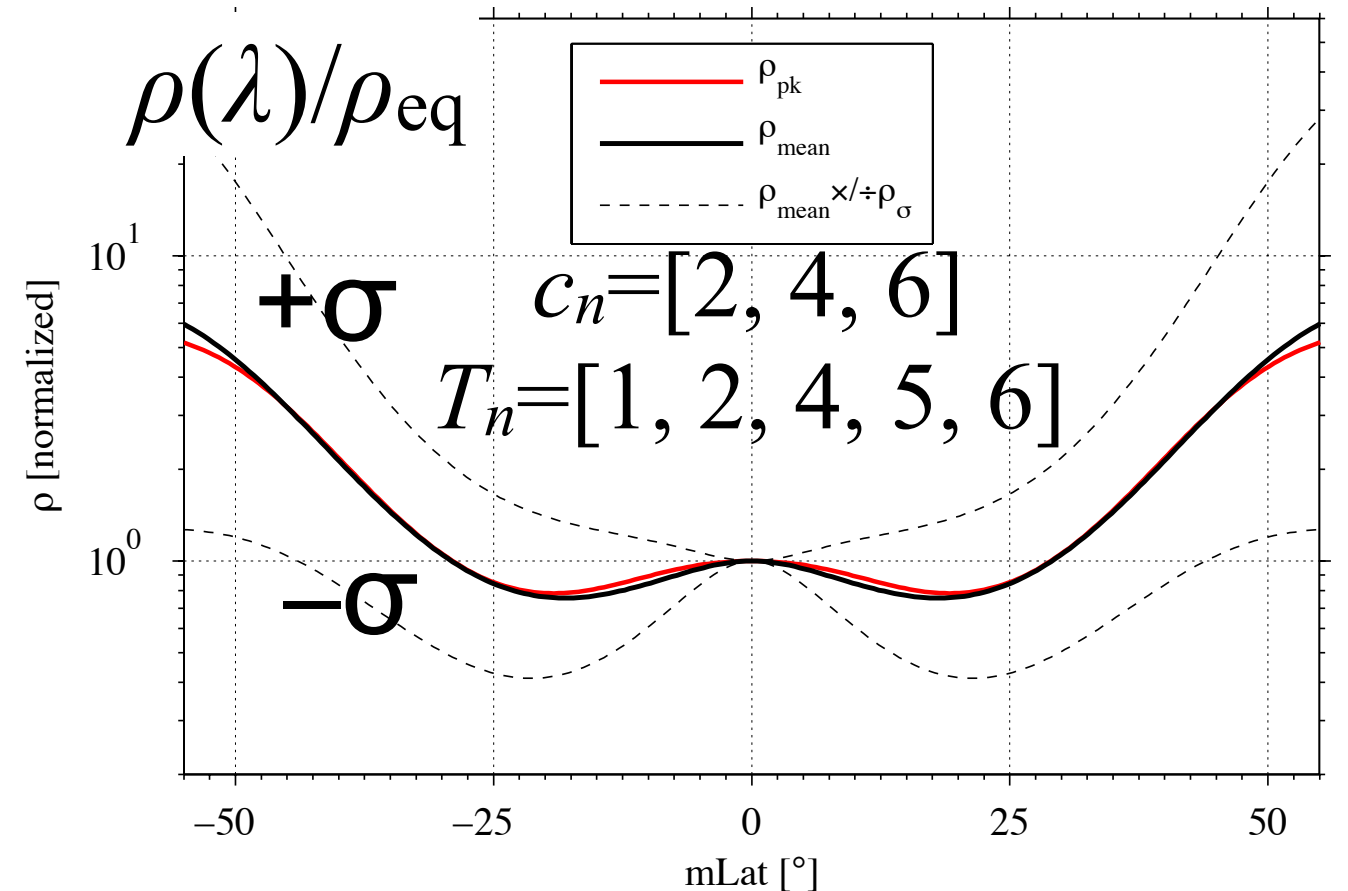
Denton et al. [2001, 2004]

## $f/f_{T3}$ Histogram

RBSP A&B  $5 < L < 6$ , All MLT

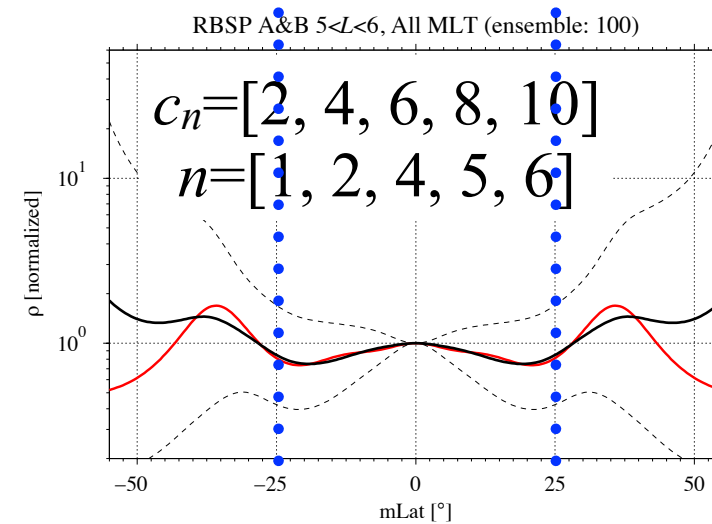
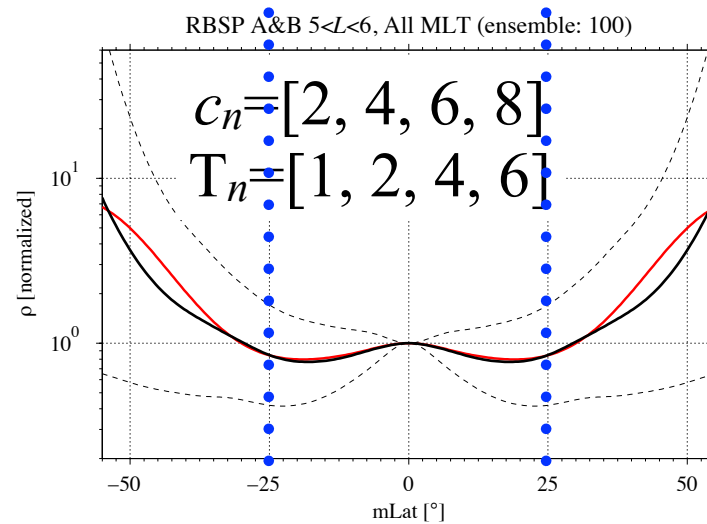
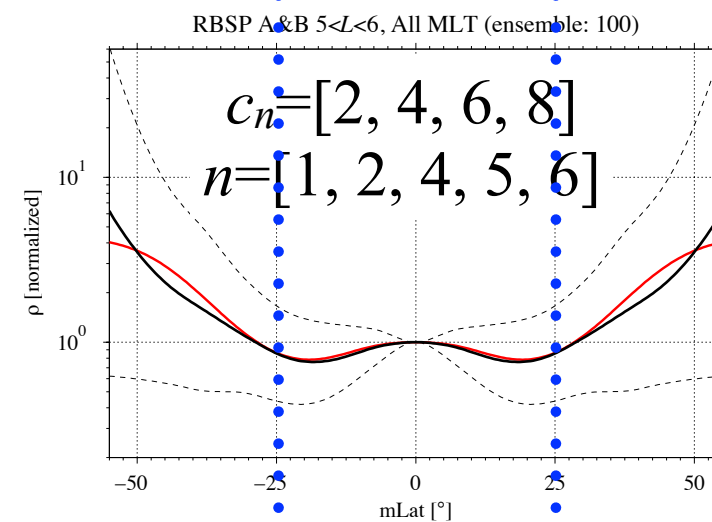
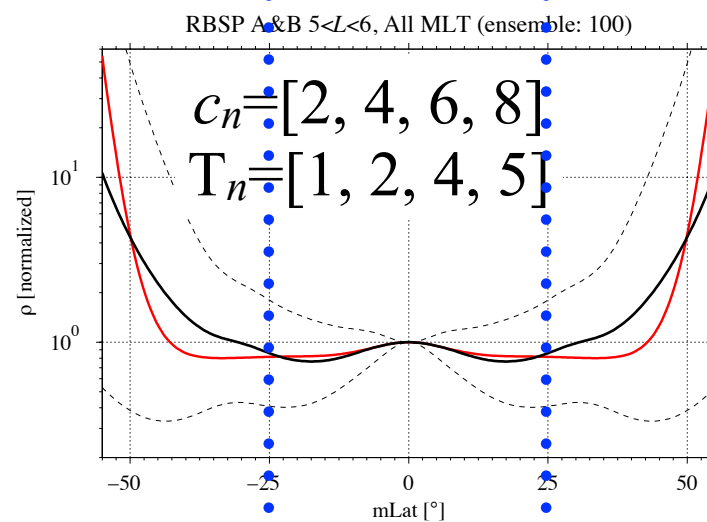
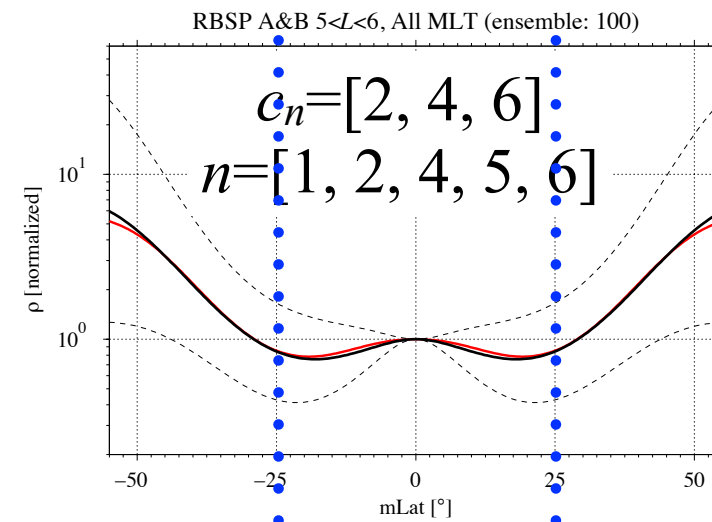
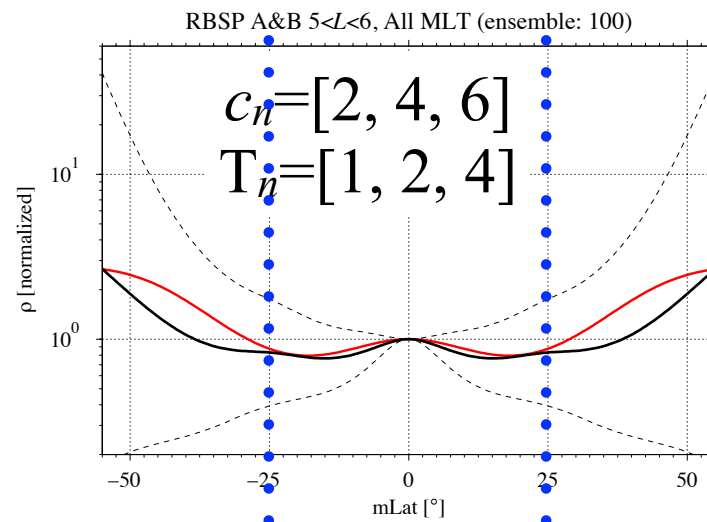


RBSP A&B  $5 < L < 6$ , All MLT (ensemble: 100)





# Statistical $\rho(\lambda)$ Variation (Cont'd)



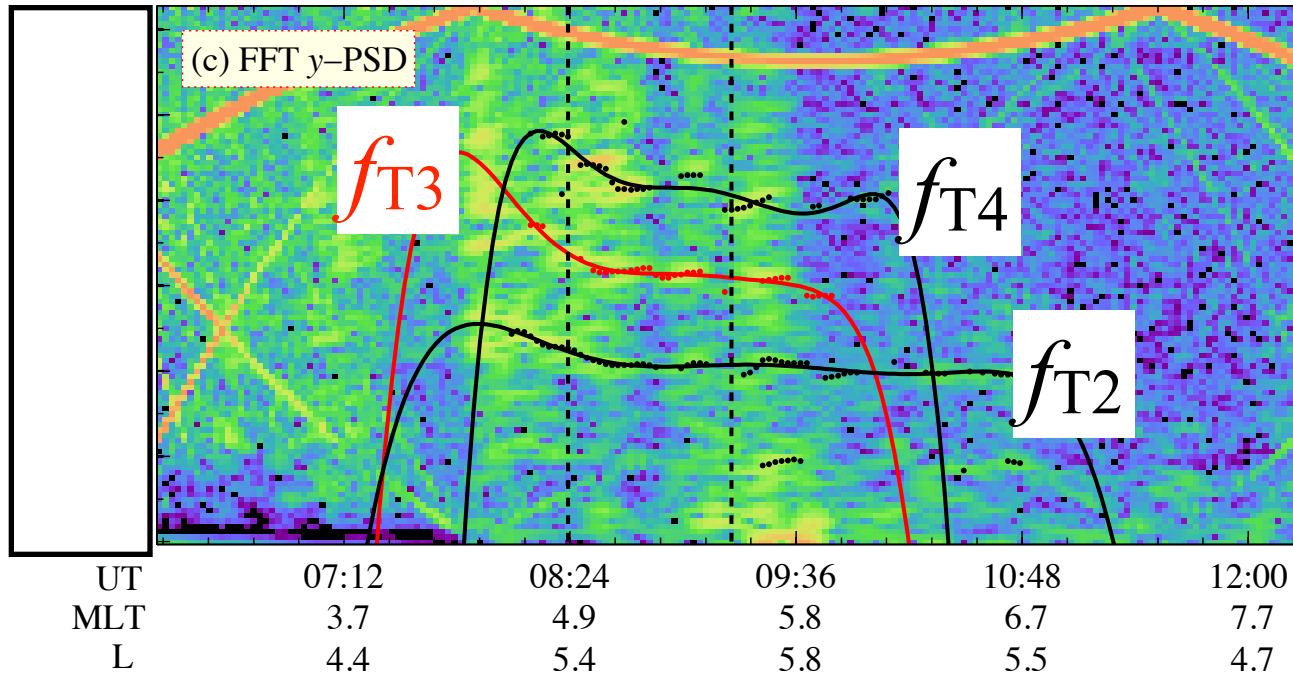
# Summary

- Explored the potential of the magneto-seismology and the potential of RBSP to derive the mass density distribution
- With the electric field from EFW, the detection rate will significantly increase
- In-situ electron density information will be very useful for interpretation
- Cross-calibration with particle measurement from HOPE instrument
- Fundamental quantity and should be understood. RBSP will help us

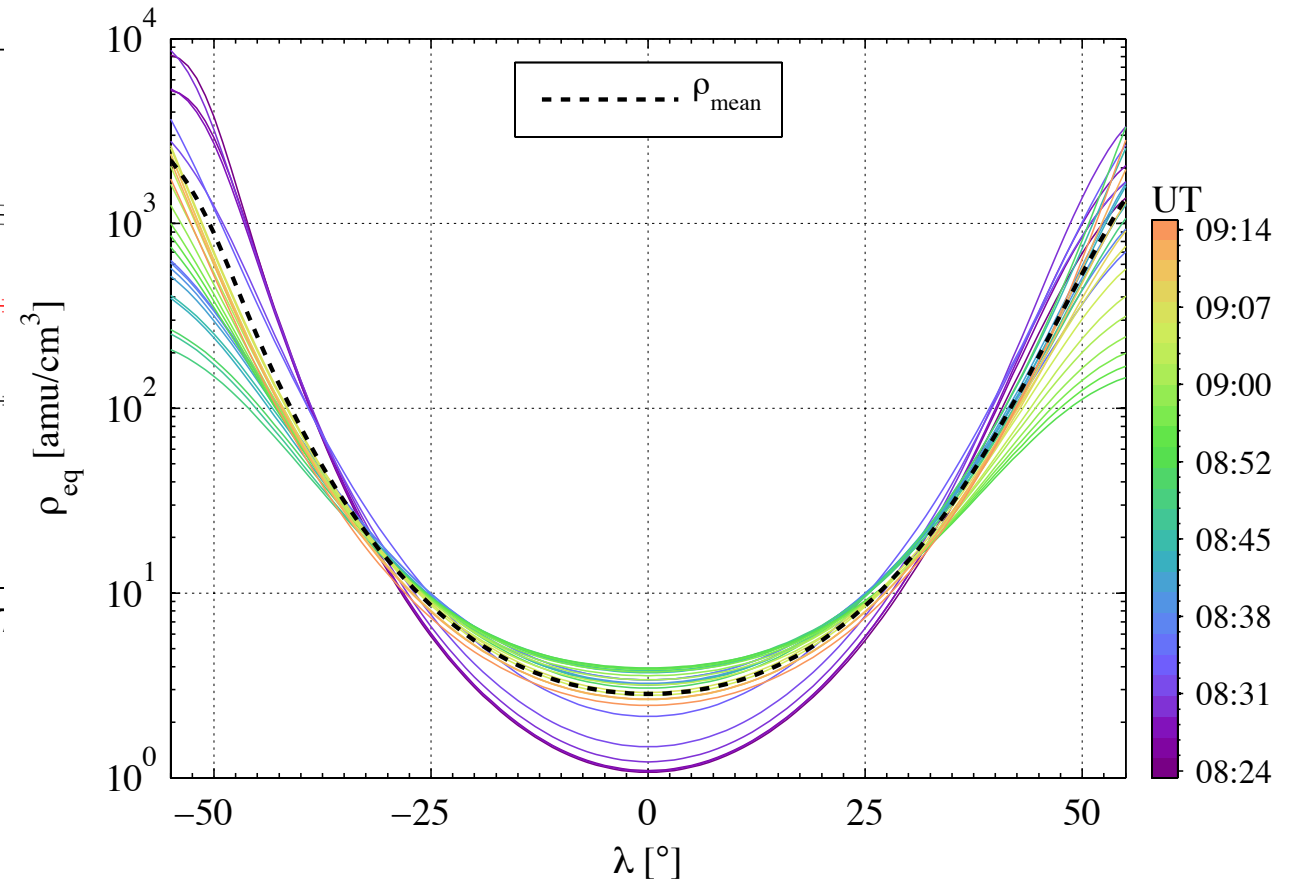
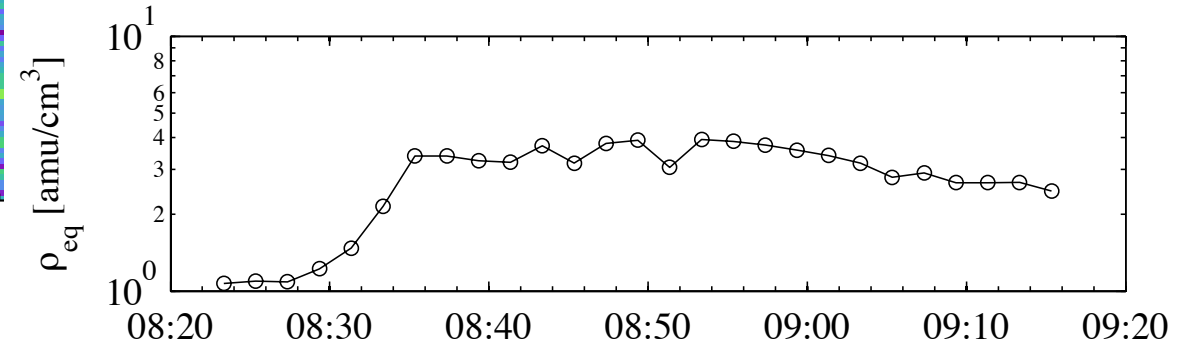
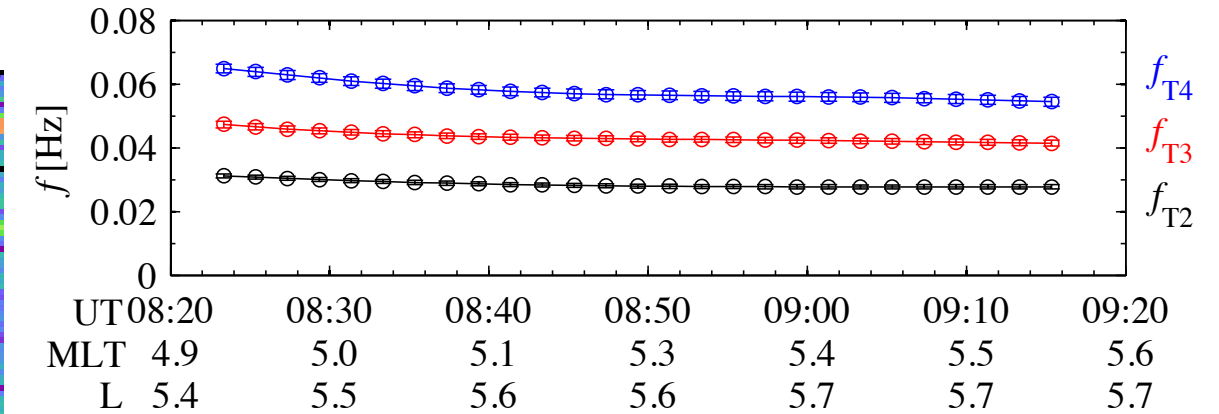
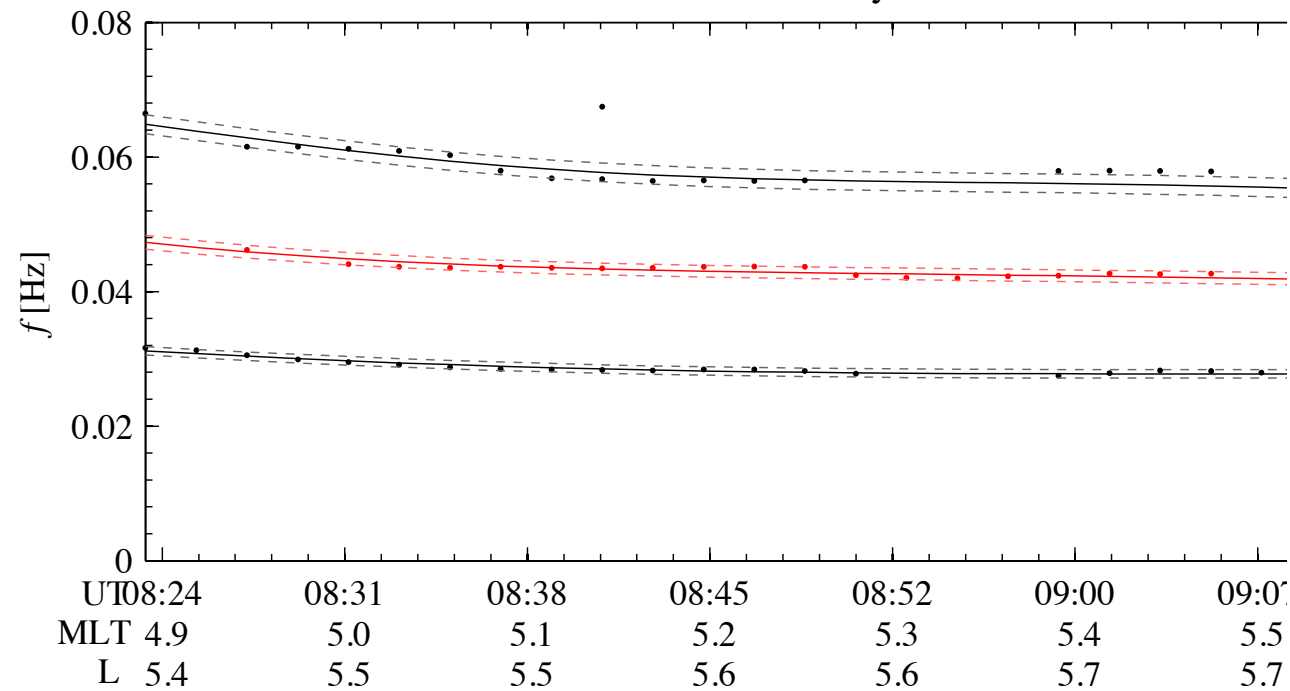
**Back-up**

# Mass Density Inversion for Event 2012-11-13 RBSP-A

RBSP-a, 13-Nov-2012



6th Order Poly. Fit

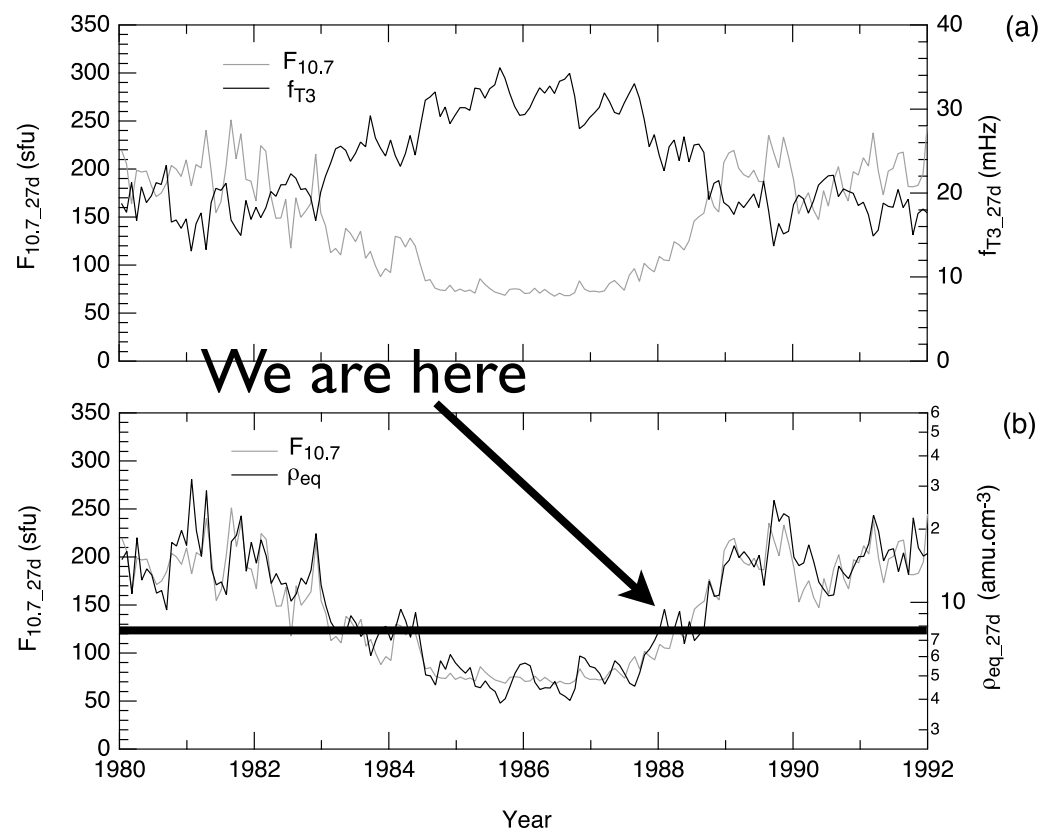


# Equatorial Mass Density, $\rho_{eq}$

$$\rho = \rho_{eq} \left( \frac{LR_E}{R} \right)^\alpha$$

with  $\alpha = 1$  (e.g. Denton et al. 2006)

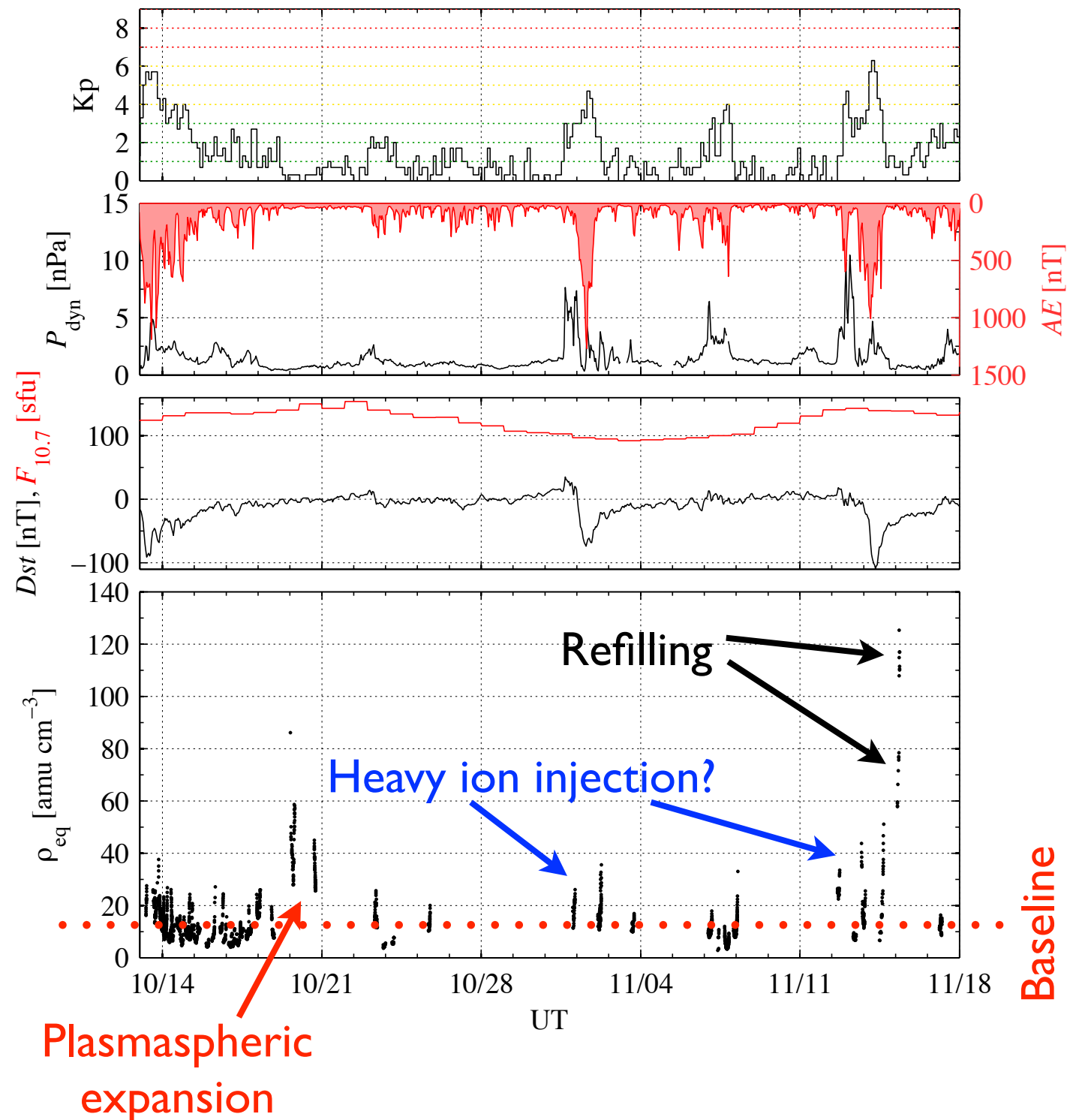
## $\rho_{eq}$ at GEO



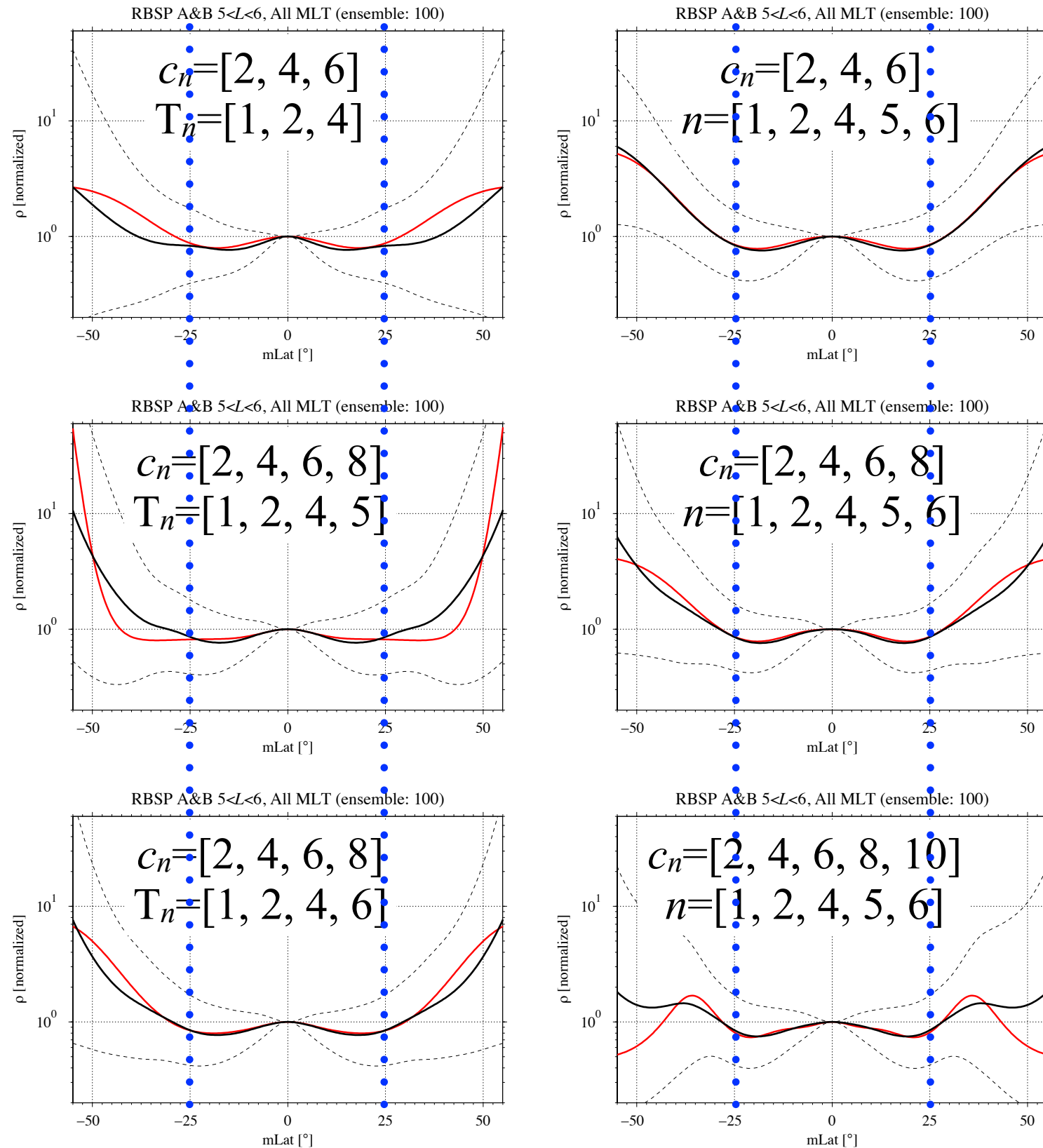
Takahashi et al. [2010]

## $\rho_{eq}$ from RBSP

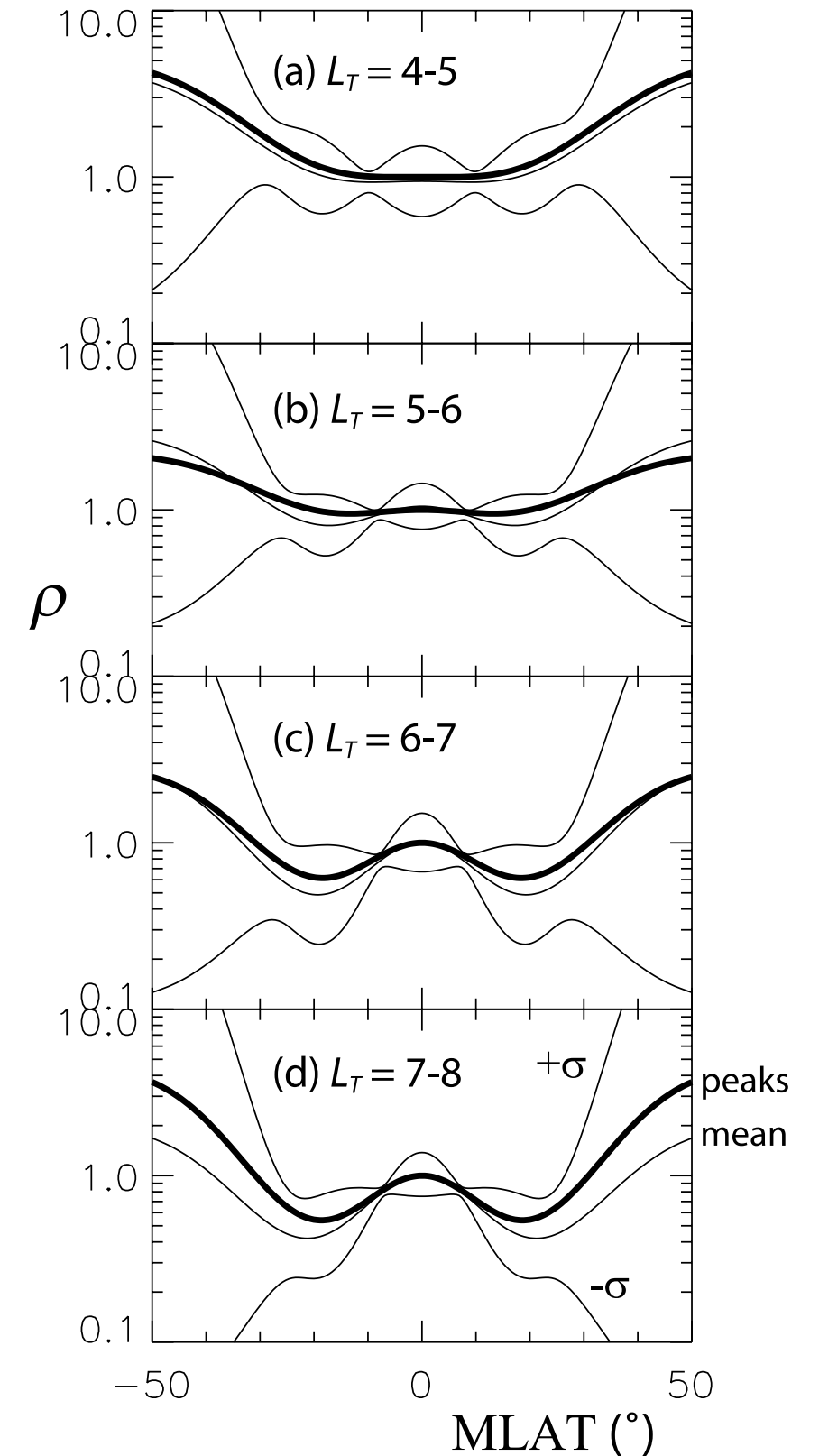
RBSP A&B  $\rho_{eq}(t, L>3)$ : 13-Oct-2012 ~ 18-Nov-2012



# Statistical $\rho(\lambda)$ Variation (Cont'd)



## CRRES



Denton et al. [2006]